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Stopping Power of Iron for Protons: Theoretical Calculations from Very Low to High Energies

Jesica P. Peralta *D, Alejandra M. P. Mendez D, Dario M. Mitnik D and Claudia C. Montanari *D

Instituto de Astronomía y Física del Espacio, CONICET and Universidad de Buenos Aires, Buenos Aires 1428, Argentina; alemendez@iafe.uba.ar (A.M.P.M.); dmitnik@df.uba.ar (D.M.M.) * Correspondence: jpperalta@iafe.uba.ar (J.P.P.); mclaudia@iafe.uba.ar (C.C.M.)

Abstract: The energy loss in iron can serve as valuable knowledge due to its extended use in technological applications and open topics in fundamental physics. The electronic structure of solid Fe is challenging, given that it is the first of the groups of transition metals with some of the *d*-electrons promoted to the conduction band while others remain bound. The low energy description, the deviation from velocity proportionality at low impact energies, and the contribution of the loosely bound *d*-electrons to the energy loss are active featured fields when it comes to the stopping in Fe. Very recent TDDFT calculations have been compared with the first stopping measurements in steel, showing surprisingly good agreement. In the present work, we applied a recent model based on the momentum distribution function of the *d*-electrons to the case of Fe. A comparison with other models is discussed, as well as with experimental data. We also highlight discrepancies among datasets regarding the stopping maximum and the need for new experimental efforts.

Keywords: stopping power; iron; transition metal; d-electrons

1. Introduction

The interaction of ions with transition metals is of significant interest in nuclear materials science, plasma physics, and energy research [1]. In particular, the energy loss of ions in inelastic collisions with the target electrons (electronic stopping power) is essential to understanding radiation damage, hydrogen embrittlement, ion implantation, and all processes related to electron structure and dynamics. The extension of ion-target systems of interest is vast, making stopping power an active field, experimentally and theoretically.

Different models have been developed over the years, from the historical works of [2,3] to studies in more recent times [4], including the free electron gas models (FEG) [5–8], realtime time-dependent density functional theory (TDDFT) [9–12], real-time solutions to the Schrödinger equation [13], binary collisional formulations [14–16], and the quantum dielectric formalisms [17–19] based on the work of Lindhard and Mermin [20,21]. All the approximations have different energy regions of validity and limitations in the number of active electrons to be considered, making the electronic stopping power a still open field, with the low-energy region and the stopping maximum being challenging and sensitive subjects.

Iron is widely used in industrial and technological applications. However, its electronic energy loss is experimentally weakly known. The stopping measurements for H and He ions in Fe were made more than thirty years ago, with discrepant groups of values around the stopping maximum (see, for example, [22–24] for H, and [25,26] for He).

Transition metals exhibit complex electronic structures that influence energy-loss processes. The first ones, groups 3–7 of the periodic table, are characterized by all their



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Copyright: © 2025 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https://creativecommons.org/ licenses/by/4.0/). valence *d*- and *s*-electrons in the conduction band, which can be described as an FEG. In contrast, in the later transition metals, groups 8–11, a fraction of the *d*-electrons remains localized and is expected to play a key role in the energy loss even at very low impact energies [27]. In this energy region, the stopping power is expected to have a linear dependence on the ion velocity. However, a departure from proportionality has been suggested for the transition metals with almost filled *d*-orbitals (groups 10 and 11) [27–30].

This work performs a detailed analysis of the stopping power of hydrogen in iron, aiming to describe it in a wide energy range. We pay special attention to the low-energy stopping power, intending to elucidate if the mentioned deviation in the linear dependence with the velocity is also present in the case of iron.

We employ a recent non-perturbative model developed by our group [31] to describe the quasi-free *d*-electron contribution to the stopping power. The total electronic stopping is calculated by including the response of the FEG, the sub-valence *d*-orbital, and the deep 1s - 3p shells. We compare the present results with all data available for H in Fe as compiled in the IAEA stopping power database [32] and with recent measurements in steel [33]. We only describe the electronic stopping power; the nuclear stopping is not included, and we assume that the low-energy experimental values have sustained it.

The theoretical models employed are described in Section 2, the results are presented and discussed in Section 3, and the conclusions are summarized in Section 4. Atomic units are used except when explicitly mentioned otherwise.

2. Theoretical Models

In the present study, we describe the electronic stopping power in the solid target. We consider that the response of electrons to the ion passage differs for the valence electrons of the metals, the loosely bound *d*-electrons, and the inner shells. Therefore, we use different formalisms for these three cases.

The valence electrons of metals are approximated as an FEG, with a homogeneous momentum distribution within the Fermi sphere. The FEG may have binary and collective excitations in response to the ion passage, and its contribution to the total stopping power is the main one at low-impact energies. As a first-order approximation, the FEG model predicts a linear dependence on the impact velocity [34]. More detailed theories [11,35] show small fluctuations on the slope. In this contribution, we use the non-perturbative model proposed in [35] based on a screened potential that depends on the ion velocity and the density of electrons in the FEG and verifies the cusp condition for the induced density of electrons following the ion passage. The FEG stopping cross-section as a function of the impact velocity v is given by the following [35,36]:

$$S_{FEG}(v) = \frac{2}{(2\pi)^3 n_a} \int \mathrm{d}\vec{p} \,\theta(p - p_F) \,v_r \frac{\vec{v}_r \cdot \vec{v}}{v} \sigma_{tr}(v_r),\tag{1}$$

where n_a is the density of target atoms, $\vec{v}_r = \vec{v} - \vec{p}$ is the relative velocity, \vec{p} is the electron momentum, $\theta(p - p_F)$ is the Heaviside step function representing the homogeneous momentum distribution, p_F is the Fermi momentum, and $\sigma_{tr}(v_r)$ is the transport cross-section in the screened potential [35]. The model described by Equation (1) is binary collisional; no collective or plasmon excitations of the FEG are included. Plasmons are known to contribute at intermediate to high impact velocities, so we employ the non-perturbative model in [35] for low impact velocities (i.e., $v \le 1.5$) and combine it with the dielectric formalism by Mermin–Lindhard [21] for higher velocities (see [37] for details).

For the contribution of the quasi-free *d*-electrons of the transition metals, we employed a recently developed model [31] based on the inhomogeneous momentum distribution function f(p) of the *d*-orbital given by

$$f(p) = \frac{(2\pi)^3}{2} |\Phi_{nd}(\vec{p})|^2,$$
(2)

with $\Phi_{nd}(\vec{p})$ being the Fourier transform of the wave functions $\phi_{nd}(\vec{r})$, normalized to the number of electrons N_e in the outer *nd*-subshell. In the case of Fe, the wave function $\phi_{3d}(\vec{r})$ employed is the Slater-type orbital expansion of the Roothaan–Hartree–Fock ground state by Bunge [38]. By using this expansion, the Fourier transform is analytical employing Flannery–Levy integrals [39]. The distribution function for the case of 3*d* electrons is

$$f(p) = \frac{(2\pi)^3}{2} \frac{N_e}{4\pi} \frac{3^2 \, 2^9}{\pi} \sum_{i=1}^5 \sum_{j=1}^5 \frac{A_i A_j \zeta_j \zeta_j \, p^4}{(\zeta_i^2 + p^2)^4 (\zeta_j^2 + p^2)^4},\tag{3}$$

where the parameters ζ_j , A_j are the coefficients of the Slater expansion, and $N_e/4\pi$ comes from the normalization of the wave function to the number of 3*d* electrons. The *d*contribution to the electronic stopping cross-section $S_d(v)$ is then expressed as

$$S_d(v) = \frac{2}{(2\pi)^3} \int \mathrm{d}\vec{p} f(p) \, v_r \frac{\vec{v}_r \cdot \vec{v}}{v} \sigma_{tr}(v_r), \tag{4}$$

where the transport cross-section is calculated using the same velocity-dependent potential proposed in Ref. [35] with the screening of a constant density of *d*-electrons $n_e = N_e n_a$.

The inner-shell contributions to the stopping power are crucial at high-impact energies. In the present work, even the deep K-shell is considered. To this end, we employed the shellwise local plasma approximation with the Levine–Mermin dielectric function (SLPA-LM) [18,37]. The stopping cross-section for a bare ion with charge Z_1 , moving with velocity v, is obtained by adding the independent contributions of each j sub-shell given by

$$S_{j} = \frac{2Z_{1}^{2}}{\pi v^{2}} \int_{0}^{\infty} \frac{dk}{k} \int_{0}^{kv} \omega \operatorname{Im}\left[\frac{-1}{\varepsilon_{j}(k,\omega)}\right] d\omega.$$
(5)

The *j*-energy-loss function is expressed as

$$\operatorname{Im}\left[\frac{-1}{\varepsilon_{j}(k,\omega)}\right] = \int \operatorname{Im}\left[\frac{-1}{\varepsilon^{\operatorname{LM}}(k,\omega;\rho_{j}(r),E_{j},\gamma_{j}(r))}\right] d^{3}\mathbf{r}, \tag{6}$$

with ε^{LM} being the Levine–Mermin (LM) dielectric response function [37], which explicitly includes the binding energy E_j , the local electron density of the atomic j sub-shell, $\rho_j(r) = |\phi_j(\vec{r})|^2$, and a local damping $\gamma_j(r) = \sqrt{\pi \rho_j(r)}$.

The total electronic stopping cross-section is calculated by adding the three independent contributions of Equations (1), (4), and (5):

$$S(v) = S_{FEG}(v) + S_d(v) + \Sigma_i S_i(v),$$

with *j* = 1*s*, 2*s*, 2*p*, 3*s*, 3*p* in the case of Fe.

The stopping power can also be expressed in terms of the friction parameter Q(v) = S(v)/v. The friction coefficient is a sensitive parameter, giving an expanded view of the energy loss problem. As mentioned above, the stopping power is expected to show a linear dependency at low-impact velocities, so Q(v) should be a constant. We will return to this in the next section, given the theoretical–experimental comparison.

3. Results and Discussion

The atomic configuration of Fe is $[Ar] 3d^64s^2$. As mentioned above, the latter transition metals, such as Fe, have some d-electrons promoted to the conduction band, while others remain bound to the target nucleus. Knowing how many electrons are part of the FEG, N_{FEG} , and how many remain bound in the *d*-subshell, N_e , is crucial for describing the energy loss. To this end, we analyzed the Hartree–Fock results for the orbital binding energies by Bunge et al. [38] and the data from reflection electron energy-loss spectroscopy in solids by Werner et al. [40].

The theoretical binding energies of Fe are displayed in Figure 1. These values for 1s - 3p are included in the SLPA-LM calculations for the inner shells given by Equation (6). It is worth mentioning that Bunge [38] calculations correspond to atoms (gas target), while we are interested in solid iron. For this reason, we also include in this figure the experimental binding energies in solids compiled in [41]. The agreement is good, except for the 3p-subshell, for which the theoretical value is 40% larger than the experimental one. No experimental binding energies are available for the 3d and 4s electrons in solid Fe. This fact is coherent with these electrons in the conduction band of the metal or with a minimal binding energy. To analyze this point, we include in Figure 1 the Fermi energy corresponding to four electrons in the FEG. This value is very close to the orbital energy $E_{3d} = 0.647$ given by Bunge [38].



Figure 1. (Color online) Electron binding energies of Fe. Hartree–Fock results by Bunge [38]—blue line and triangles; experimental values from Ref. [41]—empty circles; Fermi energy level—dashed red line.

Werner et al.'s [40] experimental data were analyzed to have a closer approach to the FEG values. The experimental plasmon frequency ω_p^{\exp} and dump γ_p^{\exp} from the first significant peak and width of the energy loss function in Ref. [40], $\omega_p^{\exp} = 0.855$ and $\gamma_p^{\exp} = 0.26$, suggest $N_{FEG} \sim 4$. Based on this value, we consider the integer $N_{FEG} = 4$, consistent with an s - d conduction band. Then, the plasmon frequency is $\omega_p = 0.795$, $r_S = 1.68$, the Fermi velocity is $v_F = 1.14$, and the Fermi energy $E_F = 0.651$.

We calculated the stopping cross-section of H in Fe by considering the independent FEG, 3*d*, and inner-shell contributions, as explained in Section 2. In Figure 2, the total electronic stopping cross-section, the FEG, and 3*d* contributions are displayed as a function of the ion impact velocity for $v < v_F$. The only experimental data for protons in Fe at these low velocities are the measurements by Arkhipov and Gott in 1969 [42], which are nicely described by the present total values. It can be noted that the FEG stopping cannot explain the data for $v \ge 0.6$, highlighting the importance of the 3*d* contribution at such low velocities. In the theoretical experimental comparison, we also include the recent measurements in eurofer97 by the Uppsala group [33]. This comparison is based on Fe being the leading steel component. For v < 0.5, our results overestimate the experimental values in [33] by less than 7%.



Figure 2. (Color online) Low-energy electronic stopping cross-section of Fe for H as a function of the impact velocity. Curves: present results for total stopping—red solid line; *d*-electron contribution—red dashed-dot line; FEG stopping—blue dashed line. Symbols: \blacktriangle [42]. Also included is \bigcirc [33] for steel (eurofer97).

The description of low-impact velocities is amplified by calculating the friction parameter Q, which should be constant for $v < v_F$, as long as the linear dependence on the impact velocity is valid. In Figure 3, we display the present results considering the total electronic stopping cross-sections and compare them with very recent TDDFT results (off-channeling) by Zhao et al. [11]. Our curve describes the experimental values by Arkhipov (1969) [42] above v = 0.5 and by Mertens (1982) [22], while Zhao et al.'s curve [11] is closer to the data given by White (1969) [24] and the recent measurements by Shams-Latifi et al. (2024) [33]. Regarding the linear behaviour, both curves are almost constant in the velocity range up to v_F , with our values being ~17% above TDDFT ones. The agreement between the two theoretical results is quite good, considering the accuracy of real-time TDDFT calculations and the sensitivity of the friction parameter.



Figure 3. (Color online) Friction parameter of Fe for H as a function of the impact velocity. Curves: thick red solid line—present total stopping; thin grey solid line—TDDFT results from Zhao [11]. Symbols: \blacktriangle [42], \blacklozenge [24], and \blacklozenge [22]. Also included is \bigcirc [33] for steel (eurofer97).

In Figure 4, we evaluate the present results in an extended energy region by presenting the electronic stopping cross-section as a function of the impact energy in the range $(0.1-5 \times 10^4)$ keV/u. Figure 4a shows the results obtained in this work for the total stopping, the FEG, 3d and inner shell contributions. The importance of the 1s - 3p ionization to the energy loss is remarkable above 40 keV/u. Present total values agree very well with the experimental data except in the region 100–200 keV/u, around the stopping maximum. Only two experimental groups measured in this energy region, White and Mueller in 1969 [24], obtained the lowest value, while Mertens and Krist in 1982 [22,23] measured a higher maximum. Despite being closer to [22,23], our present results do not follow any of the two peaks. Having new stopping measurements in Fe around the maximum would be valuable.

In Figure 4b, we compare the present total stopping cross-section with other theoretical results: the Mermin Energy-Loss Function–Generalized Oscillator Strength (MELF-GOS) values by de Vera et al. [43], and the TDDFT ones by Zhao et al. [11]. We also included the semiempirical SRIM curve [44]. The MELF-GOS results included in Figure 4b are based on the optical ELF by Werner et al. [40]. It is a perturbative model, so the observed underestimation of the data at low energies is expected. Above 30 keV/u, it describes the data very well, following the lower maximum in [24]. For energies greater than 200 keV/u, the MELF-GOS [43] values agree with the present results. The TDDFT calculations in [11] consider 14 active electrons, $3p^6 3d^6 4s^2$. The results are remarkable at low energies but are low at high energies due to the lack of deeper subshells. As expected, the semiempirical SRIM results accurately describe most data, following the higher maximum [22,23,45]. The results in Figure 4 demonstrate the strength of our proposal; it is a complete theoretical model that allows us to describe the stopping power from very low energies to high but non-relativistic ones.



Figure 4. Electronic stopping cross-section of Fe for H as a function of the impact energy. (a) Curves: present results for total stopping—red solid line; *d*-electron contributions—red dashed-dot line; FEG stopping—blue dashed line; inner-shell contribution—orange dotted line. Symbols: ● [24], ■ [46], ▼ [47], ▲ [42], ★ [48], ◀ [45], ▶ [49], ♦ [22,23], ○ [50], and ● [33] for steel (eurofer97). (b) Curves: thick red solid line—present total stopping; pink dashed-double-dot curve—MELF–GOS results from de Vera et al. [43]; thin gray solid line—TDDFT results from Zhao et al. [11]; green dashed curve—SRIM [44]. Symbols as in (a).

4. Conclusions

In this work, we examine the energy loss of protons in iron. We analyze the 3*d* electron contribution using a recent non-perturbative model based on the inhomogeneous momentum distribution. Although this contribution is essential at low-impact velocities, we found that its inclusion does not represent a departure from the linear dependence of the stopping power with the velocity. Moreover, the friction parameter obtained is almost constant for $v < v_F$. The total electronic stopping power is calculated by adding FEG, 3*d*, and 3p - 1s contributions. The present results show good agreement with the experimental values in the energy range $0.1-5 \times 10^4$ keV/u, due to the use of non-perturbative models at low energies and the dielectric formalism at intermediate to high energies, including all the deep shells. Taking into account the broadening of stopping data, it can be concluded that the present proposal manages to describe the energy loss of protons in iron in a wide range of energies.

Disagreement between experimental datasets and theoretical results is noted around the stopping maximum, making the present state of knowledge still open. It is remarkable that Fe is so under-measured. The stopping power data of protons in Fe are thirty years old, with the values around the maximum being forty years old. We emphasize the need for new stopping measurements in such a widely used material for H and also for He ions, since similar data scattering around the maximum is observed in both cases. Author Contributions: Conceptualization, J.P.P., A.M.P.M., D.M.M. and C.C.M.; methodology, J.P.P., A.M.P.M., D.M.M. and C.C.M.; software, J.P.P. and C.C.M.; validation, J.P.P., A.M.P.M., D.M.M. and C.C.M.; formal analysis, J.P.P., A.M.P.M., D.M.M. and C.C.M.; investigation, J.P.P., A.M.P.M., D.M.M. and C.C.M.; resources, J.P.P., A.M.P.M., D.M.M. and C.C.M.; data curation, J.P.P. and C.C.M.; writing—original draft preparation, J.P.P., A.M.P.M., D.M.M. and C.C.M.; writing—review and editing, J.P.P., A.M.P.M., D.M.M. and C.C.M.; writing—review and editing, J.P.P., A.M.P.M., D.M.M. and C.C.M.; project administration, D.M.M. and C.C.M.; funding acquisition, D.M.M. and C.C.M. All authors have read and agreed to the published version of the manuscript.

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